

Stress-strain relationships

Elastic strain

linear stress $\sigma_n = E \cdot e$

Poisson's ratio $\nu = -e_1/e_3$

shear stress $\sigma_s = G \cdot \gamma$

mean stress $\sigma_m = -K\Delta$

where E = Young's modulus of elasticity;

G = shear modulus of elasticity;

K = bulk modulus of elasticity;

e_1, e_3 are principal extensions of sample under uniaxial compression.

Relationships between the elastic moduli

$$G = \frac{E}{2(1 + \nu)} \quad K = \frac{E}{3(1 - 2\nu)}$$

Brittle Failure

Coulomb fracture criterion

$$\sigma_s = C + \sigma_n \tan \phi$$

where C is a constant and ϕ is the angle of internal friction.

"Byerlee's law" for movement on existing fractures

$$\sigma_s = 0.85 \sigma_n \quad (\sigma_n < 200 \text{ MPa})$$

$$\sigma_s = 50 + 0.60 \sigma_n \quad (\sigma_n > 200 \text{ MPa})$$

Viscous (Newtonian) flow

Strain rate $\dot{\epsilon} \propto \sigma_d$

where σ_d is differential stress. Alternatively: \square

$$\sigma_d = \eta \dot{\epsilon}$$

where η = viscosity.

Specific equation for diffusional creep

$$\dot{\epsilon} = A \sigma_d \exp\left(-\frac{E^*}{RT}\right) d^{-r}$$

where d is the grain size and r is 2 for grain-boundary diffusion and 3 for volume diffusion

Plastic (Von Mises) Creep

$$\sigma_d = C \quad (\text{constant})$$

Power Law Creep

$\dot{\epsilon} \propto \sigma_d^n$ where k and n are constants

or more specifically

$$\dot{\epsilon} = A \sigma_d^n \exp\left(-\frac{E^*}{RT}\right)$$

where A and n are constants for the material, E^* is the activation energy, R is the gas constant and T is the absolute temperature.

Exponential Creep

$\dot{\epsilon} \propto \exp(\sigma_d)$ where k and n are constants

or more specifically:

$$\dot{\epsilon} = A \exp(\sigma_d) \exp\left(-\frac{E^*}{RT}\right)$$

where A is a constant for the material, E^* is the activation energy, R is the gas constant and T is the absolute temperature